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# GRE® Quant Formula Guide

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✓ Fractions & Algebra

✓ Exponents & Roots

✓ Geometry & Coordinate

✓ Statistics & Probability

✓ Word Problems & Rates

✓ QC Strategy & Traps

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**FRACTIONS**

Adding — Same Denominator

$a/b + c/b = (a+c)/b$

Adding — Different Denominators

$a/b + c/d = (ad+bc)/bd$

EXAMPLE

$3/5 + 2/9 = (27+10)/45 = 37/45$

Subtracting

$a/b - c/d = (ad-bc)/bd$

Multiplying

$a/b \times c/d = ac/bd$

EXAMPLE

$3/4 \times 5/7 = 15/28$

Dividing

$a/b \div c/d = a/b \times d/c = ad/bc$

EXAMPLE

$3/8 \div 6/5 = 3/8 \times 5/6 = 5/16$

Distributive Property

$(a+c)/b = a/b + c/b$

Comparing Size — Cross Multiply

$a/b > c/d$  if  $ad > bc$

EXAMPLE

$5/7 > 4/6$  because  $30 > 28$

Squares & Roots of Fractions

$(a/b)^2 = a^2/b^2 \quad \sqrt{(x/y)} = \sqrt{x} / \sqrt{y}$

$0 < x < 1$  Property

$x^2 < x < \sqrt{x}$  when  $0 < x < 1$

**LINEAR & QUADRATIC EQUATIONS**

Factoring Out Common Factors

If a term appears in every expression, factor it out.

EXAMPLE

$6x + 6y = 12 \rightarrow 6(x + y) = 12$

Zero Product Property

If  $a \times b = 0$ , then  $a = 0$  or  $b = 0$  or both.

EXAMPLE

$x(x + 50) = 0 \rightarrow x = 0$  or  $x = -50$

General Form of a Quadratic

$ax^2 + bx + c = 0$

Must be in this form before factoring.

Factoring a Quadratic

$x^2 + bx + c = (x+p)(x+q) = 0$

- p and q **multiply** to c
- p and q **add** to b

EXAMPLE

$x^2 - 7x - 18 = 0 \rightarrow (x-9)(x+2) = 0$   
 -9 and 2 multiply to -18; add to -7

FOIL — First · Outer · Inner · Last

EXAMPLE

$(x-5)(x+3)$ : F= $x^2$  O= $3x$  I= $-5x$  L= $-15$  =  $x^2 - 2x - 15$

3 Key Quadratic Identities

- $(x+y)^2 = x^2 + 2xy + y^2$
- $(x-y)^2 = x^2 - 2xy + y^2$
- $(x+y)(x-y) = x^2 - y^2$

Difference of Squares Examples

- $x^2 - 16 = (x-4)(x+4)$
- $9x^2 - 25 = (3x-5)(3x+5)$

PEMDAS

Parentheses	Exponents
Mult & Div	Add & Sub

**PROPERTIES OF NUMBERS**

Even/Odd — Addition & Subtraction

odd+odd=even	even+even=even
even+odd=odd	odd-odd=even

Even/Odd — Multiplication

even*even=even	even*odd=even
odd*even=even	odd*odd=odd

Sign Rules

(+)(+)=(+)	(-)(-)=(+)
(+)(-)=(-)	(-)(+)=(-)

Factors

If y divides evenly into x, then y is a factor of x.

EXAMPLE

Factors of 24: 1, 2, 3, 4, 6, 8, 12, 24

Multiples

Multiples of n: n, 2n, 3n, 4n, ...

Division Formula

$x/y = \text{Quotient} + \text{remainder}/y$

EXAMPLE

$31 \div 7 = 4 + 3/7$

Range of Remainders

Remainder must be a non-negative integer **less than the divisor**.

Primes Under 100

2,3,5,7,11,13,17,19,23,29,31,37,41,43,47,53,59,61,67,71,73,79,83,89,97

Finding Number of Factors

- Prime factorize the number
- Add 1 to each exponent, multiply all results

EXAMPLE

$180 = 2^2 \times 3^2 \times 5^1 \rightarrow (2+1)(2+1)(1+1) = 18$  factors

**DIVISIBILITY RULES**

Div by	Rule
2	Last digit: 0,2,4,6,8
3	Sum of digits divisible by 3
4	Last two digits div by 4
5	Last digit: 0 or 5
6	Divisible by both 2 AND 3
8	Last 3 digits div by 8
9	Sum of digits divisible by 9
11	Alt digit sum difference div by 11

Finding the LCM

- Prime factorize each integer
- Take repeated primes with **largest** exponent
- Take all non-repeated prime factors
- Multiply everything together

EXAMPLE

$18 = 2^1 \times 3^2, 30 = 2^1 \times 3^1 \times 5^1 \rightarrow$  take  $3^2, 2^1, 5^1 \rightarrow$  **LCM = 90**

Finding the GCF

- Prime factorize each number
- Take repeated primes with **smallest** exponent
- Multiply together

EXAMPLE

Common:  $2^1, 3^1 \rightarrow$  **GCF = 6**

LCM × GCF Rule

**$LCM(x,y) \times GCF(x,y) = x \times y$**

Factorials ≥ 5!

Any factorial ≥ 5! always ends in 0 (units digit = 0).

Trailing Zeros

Count (5×2) pairs in prime factorization.

EXAMPLE

$40! \rightarrow [40/5] + [40/25] = 8 + 1 = 9$  trailing zeros

UNITS DIGIT PATTERNS

Base	Pattern
0 or 1	Always 0 or 1
2	2 → 4 → 8 → 6 (4-cycle)
3	3 → 9 → 7 → 1 (4-cycle)
4	4 → 6 (2-cycle)
5 or 6	Always 5 or 6
7	7 → 9 → 3 → 1 (4-cycle)
8	8 → 4 → 2 → 6 (4-cycle)
9	9 → 1 (2-cycle)

Perfect Squares

All prime factors have **even** exponents.

0,1,4,9,16,25,36,49,64,81,100,121,144,169,196,225

Perfect Cubes

All prime factors have exponents **divisible by 3**.

0,1,8,27,64,125,216,343,512,729,1000

Terminating Decimals

Terminates only if reduced denominator has only 2s and/or 5s.

$1/8 = 0.125$  ✓

$1/6 = 0.1666... \times$

Two Consecutive Integers

Never share prime factors. GCF of any two consecutive integers = 1.

Trailing & Leading Zeros

- Trailing zeros: count (5×2) pairs in prime factorization
- Leading zeros in  $1/x$ : if x has k digits → k-1 leading zeros (k-2 if x is a perfect power of 10)

ROOTS & RADICALS

Multiplying Radicals

$\sqrt{a} \times \sqrt{b} = \sqrt{ab}$

EXAMPLE

$\sqrt{6} \times \sqrt{10} = \sqrt{60} = 2\sqrt{15}$

Dividing Radicals

$\sqrt{a} / \sqrt{b} = \sqrt{a/b}$

EXAMPLE

$\sqrt{72} / \sqrt{8} = \sqrt{9} = 3$

Adding/Subtracting Radicals

$\sqrt{a} + \sqrt{b} \neq \sqrt{a+b}$  — you CANNOT combine unlike radicals!

You CAN add like radicals:  $3\sqrt{5} + 7\sqrt{5} = 10\sqrt{5}$

EXAMPLE

$\sqrt{9} + \sqrt{16} = 3+4 = 7 \neq \sqrt{25} = 5$

Square Root of a Binomial

$\sqrt{[(x+y)^2]} = |x+y|$

Radicals as Exponents

$\sqrt{x} = x^{1/2}$     $\sqrt[3]{x} = x^{1/3}$

$b\sqrt{x^a} = x^{a/b}$

EXAMPLE

$(\sqrt[3]{x})^2 = x^{2/3}$

Key Approximations

$\sqrt{2} \approx 1.41$

$\sqrt{3} \approx 1.73$

$\sqrt{5} \approx 2.24$

$\sqrt{7} \approx 2.65$

Large Perfect Square Roots

2k trailing zeros → root has k trailing zeros.  
 $\sqrt{10,000} = 100$     $\sqrt{40,000} = 200$

Cube Roots of Perfect Cubes

3k trailing zeros → cube root has k zeros.

EXPONENT RULES

Core Laws

- $x^1 \cdot x^2 = x^3$  (same base × → add)
- $x^1 / x^2 = x^{-1}$  (same base ÷ → subtract)
- $(x^1)^2 = x^2$  (power to power → multiply)
- $(xy)^1 = x^1y^1$
- $x \&sup0; = 1$  ( $x \neq 0$ )
- $x^{-1} = 1/x^1$

Powers of 2

$2^0=1$

$2^1=2$

$2^2=4$

$2^3=8$

$2^4=16$

$2^5=32$

$2^6=64$

$2^7=128$

$2^8=256$

$2^9=512$

$2^{10}=1024$

Other Key Powers

$3^4=81$

$3^5=243$

$4^3=64$

$5^4=625$

Special Addition Rule

- $2^n + 2^n = 2^{n+1}$
- $3^n + 3^n + 3^n = 3^{n+1}$
- Adding  $k^n$  exactly k times =  $k^{n+1}$

Adding Like Bases — Factor First!

EXAMPLE

$3^8 + 3^9 + 3^{10} = 3^8(1+3+9) = 3^8(13)$

Negative Exponents

$x^{-1} = 1/x^1$

EXAMPLES

$5^{-3} = 1/125$     $(2/3)^{-2} = (3/2)^2 = 9/4$

EXPONENT NUMBER PROPERTIES

CASE 1

Base > 1, Even Positive Exponent  
**Result is LARGER**  
 $6^2 = 36 > 6$

CASE 2

Base > 1, Odd Positive Exponent (>1)  
**Result is LARGER**  
 $4^3 = 64 > 4$

CASE 3

Base < -1, Even Positive Exponent  
**Result is LARGER (positive)**  
 $(-4)^2 = 16 > -4$

CASE 4

Base < -1, Odd Positive Exponent (>1)  
**Result is SMALLER (more negative)**  
 $(-4)^3 = -64 < -4$

CASE 5

0 < Base < 1, Even Positive Exponent  
**Result is SMALLER**  
 $(1/4)^2 = 1/16 < 1/4$

CASE 6

-1 < Base < 0, Even Positive Exponent  
**Result is LARGER (less negative)**  
 $(-1/4)^2 = 1/16 > -1/4$

CASE 7

0 < Base < 1, Odd Positive Exponent (>1)  
**Result is SMALLER**  
 $(1/4)^3 = 1/64 < 1/4$

CASE 8

-1 < Base < 0, Odd Positive Exponent (>1)  
**Result is LARGER**  
 $(-1/4)^3 = -1/4$

CASE 9

Base > 1, Fractional Exponent  
**Result is SMALLER**  
 $8^{1/3} = 2 < 8$

CASE 10

0 < Base < 1, Fractional Exponent  
**Result is LARGER**  
 $(1/9)^{1/2} = 1/3 > 1/9$

**ABSOLUTE VALUE & INEQUALITIES**

**Definition**

- If  $a \geq 0$ :  $|a| = a$
- If  $a < 0$ :  $|a| = -a$

$|75| = 75$

$|-75| = 75$

**One Absolute Value Equation**

Solve twice: positive case AND negative case.

**EXAMPLE:**  $|3x + 6| = 18$

$3x+6=18 \rightarrow x=4$   
 $-(3x+6)=18 \rightarrow x=-8$

**Two Equal Absolute Values**

If  $|A| = |B|$ , then  $A = B$  or  $A = -B$ .

**EXAMPLE:**  $|4x+2| = |2x+10|$

$4x+2=2x+10 \rightarrow x=4$   
 $4x+2=-(2x+10) \rightarrow x=-2$

**Adding Absolute Values**

$|a+b| \leq |a| + |b|$

Equality holds when a,b same sign or one is zero.

**Subtracting Absolute Values**

$|a-b| \geq |a| - |b|$

**Inequality Rules**

- Add/subtract: sign stays the same
- $\times$  or  $\div$  by **positive**: sign stays
- $\times$  or  $\div$  by **negative**: **FLIP the sign!**

**Compound Inequalities**

$|x| < k \rightarrow -k < x < k$

$|x| > k \rightarrow x < -k \text{ or } x > k$

**WORD PROBLEMS**

**Key Translations**

English	Math
is / was / has been	=
more / older	+
less / fewer / younger	-
times / of / factor of	$\times$
less than	-
as many as	$\times$
what / some number	variable

**Price Per Item**

$\text{Price/item} = \text{Total Cost} \div \text{\# of Items}$

**Profit Equation**

$\text{Profit} = \text{Revenue} - \text{Total Cost}$

→ Total Cost = Fixed Costs + Variable Costs

**Simple Interest**

$I = P \times r \times t$

P = principal, r = annual rate, t = years

**Compound Interest**

$A = P(1 + r/n)^{nt}$

- n = times compounded per year
- t = time in years

**Linear Growth**

$F_n = p + k \cdot n$

→ p = initial value, k = increase per period

**Consecutive Integers**

- Integers: x, x+1, x+2, ...
- Even/Odd: x, x+2, x+4, ...
- Multiples of k: x, x+k, x+2k, ...

**RATE & WORK PROBLEMS**

**Distance–Rate–Time**

**Distance = Rate  $\times$  Time**

$T = D / R$

$R = D / T$

**Average Rate Formula**

**Avg Rate = Total Distance / Total Time**

Never just average two speeds! Always use total D and total T.

**Converging / Diverging**

$D_1 + D_2 = D_{\text{total}}$  (moving toward each other)

**Round-Trip & Catch-Up**

- Round-trip:  $D_{\text{out}} = D_{\text{return}}$
- Catch-up:  $D_1 = D_2$  at meeting point

**Catch & pass: Time =  $\Delta$ Distance /  $\Delta$ Rate**

**WORK PROBLEMS**

**Work Formula**

**Work = Rate  $\times$  Time**

$\text{Rate} = W/T$

$\text{Time} = W/R$

**Individual Work Rate**

a jobs in b hours → Rate = a/b jobs per hour.

**EXAMPLE**

12 reports in 4 days → Rate = 3/day

**Combined Workers**

$\text{Work}_A + \text{Work}_B = \text{Work}_{\text{Total}}$

$1/T_{\text{combined}} = 1/T_A + 1/T_B$

**RATIOS**

**3 Ways to Write a Ratio**

- cats/dogs = 5/3
- cats : dogs = 5 : 3
- cats to dogs = 5 to 3

**Part-to-Total Ratio**

If part1=x and part2=3x:  
 part1/total = x/(4x) = 1/4

**Combining Ratios — Use LCM**

**EXAMPLE**

xy:2:5 and x:z=3:7  
 LCM(2,3)=6 → x:y:z = **6:15:14**

**PERCENT WORD PROBLEMS**

**Converting**

- Fraction → %: divide,  $\times 100$ , add %
- % → decimal: drop %,  $\div 100$

**Percent Of**

**n% of x =  $(n/100) \times x$**

**Percent Less / Greater Than**

- n% less than y →  $\times (1 - n/100)$
- n% greater than y →  $\times (1 + n/100)$

**30% less →  $\times 0.70$**

**30% more →  $\times 1.30$**

**Percent Change Formula**

**% Change =  $(\text{Final}-\text{Initial})/\text{Initial} \times 100$**

**What Percent Translation**

**"a is what % of b?" →  $(a/b) \times 100$**

**Successive Percents**

Two consecutive % changes do NOT simply add!  
 +20% then -20%:  $100 \rightarrow 120 \rightarrow 96$  (net -4%)

STATISTICS

Arithmetic Mean

Mean = Sum of all terms / # of terms

Evenly Spaced Sets

Mean = Median in any evenly spaced set.

Mean = (Highest + Lowest) / 2

Counting Integers (Inclusive)

Count = Highest - Lowest + 1

EXAMPLE

Integers 12–47:  $47 - 12 + 1 = 36$

Counting Multiples in a Range

Count = (High\_mult - Low\_mult) / k + 1

Weighted Average

WA =  $\Sigma(\text{value} \times \text{freq}) / \text{Total frequency}$

WA is always closer to the data point with greater weight.

Median

- Order the set first!
- Odd # of terms: position =  $(n+1)/2$
- Even # of terms: avg of  $n/2$  and  $(n/2+1)$  positions

Mode & Range

- Mode: most frequently appearing value
- Range = Highest - Lowest

Standard Deviation Rules

- Add/subtract a constant → SD unchanged
- Multiply/divide each term by k → SD × k (or ÷k)

High = mean + x·SD    Low = mean - x·SD

OVERLAPPING SETS

Two-Set Formula

#(A or B) = #A + #B - #(A and B)

Two-Set with Neither

Total = #A + #B - #Both + #Neither

Double Matrix — Two Binary Attributes

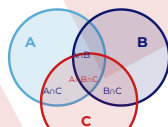
	Has X	No X	Total
Has Y			
No Y			
Total			

Three-Set — Unique Count Known

Total = A\_only + B\_only + C\_only + (A∩B)\_only + (A∩C)\_only + (B∩C)\_only + A∩B∩C + Neither

Three-Set — Unique Count Unknown

Total = #A+#B+#C - #(exactly 2) - 2\*#(all 3) + #Neither



COMBINATIONS & PERMUTATIONS

Combinations — Order Does NOT Matter

${}_nC_k = n! / [(n-k)! \times k!]$

EXAMPLE

Choose 3 from 7:  ${}_7C_3 = 7! / (4! \times 3!) = 35$

Permutations — Order DOES Matter

${}_nP_k = n! / (n-k)!$

EXAMPLE

Arrange 3 from 7:  ${}_7P_3 = 7! / 4! = 210$

Permutations with Repeated Items

$P = N! / (r_1! \times r_2! \times \dots \times r_n!)$

EXAMPLE

Arrange PEPPER:  $6! / (3! \times 2! \times 1!) = 60$  ways

Circular Arrangements

Circular arrangements =  $(k - 1)!$

EXAMPLE

5 people around a table:  $(5-1)! = 24$  ways

Counting Principle (AND Rule)

If A has m outcomes and B has n outcomes:  $m \times n$  total.

C vs. P — Which to Use?

Committee → C

Ordered list → P

Team selection → C

Different prizes → P

PROBABILITY

Basic Formula

$P = \text{Favorable} / \text{Total Outcomes}$

Sample Space Rule

All probabilities in a sample space must sum to 1.

Complementary Events

$P(A) + P(\text{not } A) = 1$

$P(\text{at least 1}) = 1 - P(\text{none})$

P(A AND B)

- Independent:  $P(A \text{ and } B) = P(A) \times P(B)$
- Dependent:  $P(A \text{ and } B) = P(A) \times P(B|A)$

EXAMPLE

$P(2 \text{ heads}) = 1/2 \times 1/2 = 1/4$

P(A OR B)

- Mutually exclusive:  $P(A \text{ or } B) = P(A) + P(B)$
- Not mutually exclusive:  $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$

Conditional Probability

$P(B|A) = P(A \text{ and } B) / P(A)$

Read as: probability of B given A occurred.

Probability with Combinations

$P = {}_nC_k(\text{favorable}) / {}_nC_k(\text{total})$

EXAMPLE

$P(2 \text{ red from } 5R+3B) = {}_5C_2 / {}_8C_2 = 10/28 = 5/14$

ANGLES & TRIANGLES

Angle Types

Acute < 90°

Right = 90°

Obtuse 90-180°

Straight = 180°

Full rotation = 360° | Supplementary angles sum to 180°

Parallel Lines + Transversal

- Vertical angles are equal
- Corresponding angles are equal
- Alternate interior angles are equal
- Co-interior angles sum to 180°

Triangle Rules

- Interior angles sum to 180°
- Exterior angle = sum of 2 non-adjacent interior angles

Triangle Inequality: sum of any 2 sides must be greater than the 3rd side.

Area of a Triangle

$Area = \frac{1}{2} \times base \times height$

Pythagorean Theorem

$A^2 + B^2 = C^2$

Pythagorean Triples

3-4-5

5-12-13

8-15-17

7-24-25

Any multiple is also a triple (e.g. 6-8-10).

45-45-90 Triangle

Legs: x Hypotenuse:  $x\sqrt{2}$

Square diagonal = side  $\times \sqrt{2}$

30-60-90 Triangle

Short: x Long:  $x\sqrt{3}$  Hyp:  $2x$

Equilateral triangle altitude → two 30-60-90 triangles.

Equilateral Triangle Area

$Area = (side^2 \times \sqrt{3}) / 4$

POLYGONS

Interior Angles Sum

$Sum = (n - 2) \times 180^\circ$

Shape	Sides	Sum
Triangle	3	180°
Quadrilateral	4	360°
Pentagon	5	540°
Hexagon	6	720°
Octagon	8	1080°

Exterior angles of ANY polygon always sum to 360°.

Rectangle

- Perimeter =  $2L + 2W$
- Area =  $L \times W$
- Diagonal =  $\sqrt{L^2 + W^2}$

Fixed perimeter → max area = square  
Fixed area → min perimeter = square

Square

- Perimeter =  $4s$  Area =  $s^2$
- Diagonal =  $s\sqrt{2}$

Parallelogram & Trapezoid

→ Parallelogram Area = base  $\times$  height

$Trapezoid Area = \frac{1}{2}(b_1 + b_2) \times h$

Hexagon

$Area = (\frac{3\sqrt{3}}{2}) \times s^2$

CIRCLES

Core Formulas

$Area = \pi r^2$  Circumference =  $2\pi r$

Diameter =  $2r$ . Chord: both endpoints on the circle.

Arc Length

$Arc = (Angle / 360) \times 2\pi r$

Sector Area

$Sector = (Angle / 360) \times \pi r^2$

Inscribed Angles

- Central angle =  $2 \times$  inscribed angle (same arc)
- Inscribed angle in semicircle =  $90^\circ$

Triangle inscribed with one side as the diameter is always a right triangle.

Circular Ring Area

$Area = \pi(R_{outer}^2 - R_{inner}^2)$

3D GEOMETRY

Cylinder ( $r$  = radius,  $h$  = height)

- Volume =  $\pi r^2 h$
- Surface Area =  $2\pi r^2 + 2\pi r h$

Cube ( $s$  = side)

- Volume =  $s^3$  Surface Area =  $6s^2$
- Diagonal =  $s\sqrt{3}$

Rectangular Solid ( $L, W, H$ )

- Volume =  $L \times W \times H$
- Surface Area =  $2(LW + WH + LH)$
- Diagonal =  $\sqrt{L^2 + W^2 + H^2}$

COORDINATE GEOMETRY

Slope Formula

$m = (y_2 - y_1) / (x_2 - x_1)$  = Rise/Run

Slope-Intercept Form

$y = mx + b$  ( $m$  = slope,  $b$  = y-intercept)

Positive: ↗

Negative: ↘

Zero: —

Undefined: |

Parallel & Perpendicular

- Parallel: same slope, different y-intercept
- Perpendicular:  $m_1 \times m_2 = -1$  (negative reciprocals)

Distance & Midpoint

$D = \sqrt{[(x_2 - x_1)^2 + (y_2 - y_1)^2]}$

$Midpoint = ((x_1 + x_2) / 2, (y_1 + y_2) / 2)$

Reflections

x-axis:  $(x, y) \rightarrow (x, -y)$

y-axis:  $(x, y) \rightarrow (-x, y)$

origin:  $(x, y) \rightarrow (-x, -y)$

$y=x$ :  $(x, y) \rightarrow (y, x)$

FUNCTIONS & SEQUENCES

Arithmetic Sequence

$a_n = a_1 + (n-1)d$

→  $d$  = common difference

$Sum S_n = (n/2)(a_1 + a_n)$

Geometric Sequence

$a_n = a_1 \times r^{n-1}$

→  $r$  = common ratio

EXAMPLE

4,12,36,108 ( $r=3$ ):  $a_5 = 4 \times 3^4 = 324$

**QC: THE 4 ANSWER CHOICES**

These are **always** the same — memorize them cold.

**A — Quantity A is greater**

A is ALWAYS greater under every possible condition

**B — Quantity B is greater**

B is ALWAYS greater under every possible condition

**C — The two quantities are equal**

They are ALWAYS equal under every possible condition

**D — Cannot be determined**

The relationship CHANGES depending on the values used

If you get two **different answers** when plugging in different values — the answer is always **D**.

**The Epic QC Attack Plan**

- Simplify both sides first — treat like an equation
- Look for a constraint (integer? positive? non-zero?)
- Plug in strategic numbers to test
- If answers differ across values → pick D immediately
- If quantities look equal, verify with an edge case
- Don't reach for the calculator — most QC questions don't need it

**THE 7 CLASSIC QC TRAPS**

**TRAP 1 — Assuming Variables Are Positive**

If the problem doesn't say  $x > 0$ , test  $x = 0$ ,  $x = -1$ , and  $x = 1/2$ . Zero and negatives destroy most "obvious" answers.

QA:  $x$  QB:  $3x$  → Looks like B, but  $x = 0$  makes them equal,  $x = -1$  flips it. Answer: D

**TRAP 2 — Squaring Changes the Comparison**

$x^2$  is NOT always  $> x$ . When  $0 < x < 1$ ,  $x^2 < x$ . When  $x < 0$ ,  $x^2 > 0 > x$ . Always test fractions and negatives with powers.

QA:  $x^2$  QB:  $x$  →  $x = 2$  gives A wins;  $x = 0.5$  gives B wins. Answer: D

**TRAP 3 — Geometry Not Drawn to Scale**

GRE figures are **NOT necessarily drawn to scale** unless stated. A triangle that looks right-angled is not — unless the problem says so. Redraw with extreme values on your scratch paper.

Trap: assuming equal-looking segments are equal, or a shape is regular when it isn't.

**TRAP 4 — "Impossible" Geometry IS Solvable**

QC geometry that looks unsolvable often has a hidden constraint that pins the answer. Check for parallel lines, isosceles triangles, angle rules, or a fixed total (e.g. angles in a triangle sum to  $180^\circ$ ) that uniquely determines the answer.

If a constraint fixes the shape, the answer is A, B, or C — not D.

**TRAP 5 — The "Too Easy" Trap**

If a QC looks instantly obvious, there's almost certainly a twist. Slow down. Check for hidden constraints, special cases ( $x = 0$ ,  $x = 1$ ), or a diagram that's misleading you.

**TRAP 6 — Ignoring the Constraint**

The centered information above the two quantities is a **constraint**, not flavor text. It often changes everything. Write it down. Many QC problems are designed so that ignoring the constraint leads directly to the wrong answer.

**TRAP 7 — Fraction / Decimal Behavior**

Fractions between 0 and 1 behave counterintuitively: multiplying makes them **smaller**, squaring makes them **smaller**, taking the square root makes them **larger**. Always test  $x = 1/2$  when fractions could be involved.

**STRATEGIC PLUG-IN NUMBERS**

When variables appear in QC, systematically test these values in this order:

**THE EPIC 5**  
0 1 -1 1/2 2

Test these every time variables appear with no constraints

Value	Why it's useful
0	Kills multiplication, collapses exponents to 0
1	Powers stay the same: $1^2=1^3=1$
-1	Flips inequalities, reveals sign traps
1/2	Fractions: squaring makes smaller, rooting makes larger
2	Simple positive integer baseline
-1/2	Negative fraction: combines sign + fraction traps
Large (100)	Tests behavior at extremes

**How to Use Plug-In Results**

- Same answer every time → strong signal for A, B, or C
- Different answers across values → answer is **D**
- Two values give the same result but a third differs → **D**
- Only need **two different outcomes** to confirm D

**Simplify Before Plugging In**

Treat QC like an equation: add, subtract, multiply, or divide the same thing from both sides to simplify. Only multiply/divide by a **positive** number — if the sign is unknown, you cannot do this.

**EXAMPLE**

QA:  $3x + 6$  QB:  $3x + 9$   
Subtract  $3x$  from both → QA: 6 QB: 9 → Answer: **B** always

**GRE QUESTION TYPES: QUANT**

**Quantitative Comparison (QC)**

Compare Quantity A vs Quantity B. Same 4 choices every time. About half of all quant questions.

**Problem Solving (PS)**

Standard MCQ: pick one answer from 5, or select all that apply (checkboxes), or enter a numeric value directly.

**Data Interpretation (DI)**

2–3 questions based on a shared chart, table, or graph. Read axes carefully. Watch for "approximate" and "closest to."

**GRE TEST STRUCTURE**

Section	Questions	Time
Analytical Writing	1 essay	30 min
Verbal 1	12 questions	18 min
Quant 1	12 questions	21 min
Verbal 2*	15 questions	23 min
Quant 2*	15 questions	26 min

\*Adaptive: harder if you did well in section 1. Score range: 130–170 per section.

**VERBAL QUESTION TYPES (QUICK REF)**

**Text Completion (TC)**

1–3 blanks. Fill each blank independently. No partial credit — all blanks must be correct.

**Sentence Equivalence (SE)**

Select **2** words that both complete the sentence AND produce sentences alike in meaning.

**Reading Comprehension (RC)**

Single-answer MC, multi-answer (select all), and sentence highlight. Passage types: argument, social science, natural science, humanities.

**GRE SCORING**

130–170 Quant

130–170 Verbal

0–6 Writing

1-pt increments